## A CORRECTION OF SOME THEOREMS ON PARTITIONS

## BY PETER HAGIS, JR.

Theorem 4 in [1] gives a convergent series representation for  $p_a(n)$ , the number of partitions of a positive integer n into positive summands of the form  $mp \pm a_j$ . Here p is an odd prime and  $a_j$  is an element of a set a consisting of r positive residues of p each of which is less than p/2. It is stated that the theorem holds for  $n \ge A/12p$ , where  $A = rp^2 - 6 \sum_{j=1}^r a_j(p-a_j)$ . In the proof of this theorem the estimate  $O(n^{1/3}k^{2/3+\epsilon})$  is used for certain complicated exponential sums. The proof of this estimate given in Theorem 2 of [1] depends on the fact that (A-12pn,k) = O(n). This is clearly false (in general) if A = 12pn since (0,k) = k. Thus, Theorem 4 of [1] has been established only if n > A/12p.

Similar remarks apply to Theorem 6 in [2] in which a convergent series is obtained for  $q_a(n)$ , the number of partitions of n into distinct positive summands of the form  $mp \pm a_j$ . Here it is asserted that the theorem holds for  $n \ge -A/12p$ . However, the proof given is valid only if n > -A/12p. For the argument used to establish the required estimate  $O(n^{1/3}k^{2/3+\epsilon})$  for the exponential sums involved does not hold if A = -12np. Thus, until (if ever) the necessary estimates contained in Theorems 2 and 3 of [1] and Theorems 2 through 5 of [2] can be justified for  $n = \pm A/12p$  we must exclude these values of n from consideration.

We conclude by giving a simple necessary condition for  $A = \pm 12pn$ . From the definition of A given above and the fact that either  $a_j$  or  $p - a_j$  is even we see that if  $A = \pm 12pn$  then 12|r.

## REFERENCES

- 1. P. Hagis, Jr., A problem on partitions with a prime modulus  $p \ge 3$ , Trans. Amer. Math. Soc. 102 (1962), 30-62.
- 2. ——, On a class of partitions with distinct summands, Trans. Amer. Math. Soc. 112 (1964), 401-415.

TEMPLE UNIVERSITY,
PHILADELPHIA, PENNSYLVANIA